Automatic Security Analyses of Network Protocols with Tamarin-Prover Introductory Talk

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## Outline

#### Motivation

Tamarin-Prover Overview Language and Environment State Demo

Goals for the Lab

$$\frac{-1}{1} = \frac{1}{-1}$$

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## Experts on Security Proofs<sup>1</sup>

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 "In our opinion, many proofs in cryptography have become essentially unverifiable. Our field may be approaching a crisis of rigor. [...] game-playing may play a role in the answer." Bellare and Rogaway 2004

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# Experts on Security Proofs<sup>1</sup>

- "In our opinion, many proofs in cryptography have become essentially unverifiable. Our field may be approaching a crisis of rigor. [...] game-playing may play a role in the answer." Bellare and Rogaway 2004
- "We generate more proofs than we carefully verify (and as a consequence some of our published proofs are incorrect)." Halevi 2005

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of statements or security properties for a given protocol.

Goal: Extensible framework for plug-and-play security.

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Our Goal: Analyse IPSec protocol using automatic provers

### Tamarin



Brocken Inaglory, edited by Fir0002, edited by Brocken Inaglory (https://commons.wikimedia.org/wiki/File:Tamarin\_portrait\_2\_edit3.jpg) https://creativecommons.org/licenses/by-sa/4.0/legalcode

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of statements or security properties for a given protocol. (*Tamarin-Prover Manual*, Basin et al. 2018)

However, Tamarin-Prover is not guaranteed to terminate.

Anatomy of Tamarin Scripts

A script for Tamarin-Prover is a text file with the extension . spthy.

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# stuff goes here

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- Variables, Constants
- Function symbols
- Equations
- Rules
- Axioms
- Lemmata

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During execution, the state of Tamarin is a multiset of facts.

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  - m messages, e.g. encrypted data, plaintexts
  - ~x random variables, e.g. nonces, private keys
  - \$S publicly known variables, e.g. server identity
  - #i temporal variable, e.g. to determine the order in which events happened

#### rule RuleIdentifier:

- [ Premise Facts ] --[ Action Facts ]->
- [ Conclusion Facts ]

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### rule RuleIdentifier: let key = value # ... in [ Premise Facts ] --[ Action Facts ]-> # can be abbreviated by --> [ Conclusion Facts ]

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rule RuleIdentifier:
    let
        key = value
        # ...
in
    [ Premise Facts ]
--[ Action Facts ]-> # can be abbreviated by -->
    [ Conclusion Facts ]
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The facts In(...) and Out(...) represent messages received or sent over an unprotected channel, respectively.

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rule RuleIdentifier:
    let
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        # ...
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    [ Premise Facts ]
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The facts In(...) and Out(...) represent messages received or sent over an unprotected channel, respectively. The fact Fr(...) generates fresh variables.

Create Something from Nothing

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rule RuleConstant:
 [ ] --> [ Fact('a') ]

Create Something from Nothing

State (multiset of facts):

rule RuleConstant:
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Create Something from Nothing

Trace:

State (multiset of facts):

rule RuleConstant:
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Trace: RuleConstant

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Fact('a')

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- Fact('a')

rule RuleConsumer:
 [ Fact('a') ] --> [ NewFact('b') ]

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- Complete control over the network: sending, receiving messages is done by the attacker.
- Usually, access to a reveal oracle

Public Channel vs. State

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```
rule CreateIdentity:
    [ Fr(~sk) ]
    -->
    [ !Id($A,~sk, ) ]
```

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rule CreateIdentity:
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builtins: diffie-hellman

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rule GetPk:
 [ !Id(A,sk,pk) ]
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 [ Out(<A, pk>) ]

Public Channel vs. State

Trace:

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rule CreateIdentity:
    [Fr(~sk)]
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                               Public Channel:
rule GetPk:
    [ !Id(A,sk,pk) ]
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Public Channel vs. State

Trace: Createldentity

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Public Channel:

Public Channel vs. State

Trace: Createldentity, GetPk

State:

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Public Channel:

Public Channel vs. State

Trace: Createldentity, GetPk, irecv

State:

```
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```

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 -->
 [ Out(<A, pk>) ]

- !Id(\$A,~sk,'g'^~sk)
- !KD(<A,pk>)

Public Channel:

<A,pk>

Public Channel vs. State

Trace: Createldentity, GetPk, irecv, coerce

State:

```
builtins: diffie-hellman
```

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    [ Fr(~sk) ]
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rule GetPk:
 [ !Id(A,sk,pk) ]
 -->
 [ Out(<A, pk>) ]

- !Id(\$A,~sk,'g'^~sk)
- !KD(<A,pk>)
- !KU(<A,pk>)

Public Channel:

<A,pk>

Public Channel vs. State

Trace: Createldentity, GetPk, irecv, coerce, isend

State:

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builtins: diffie-hellman
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- !Id(\$A,~sk,'g'^~sk)
- !KD(<A,pk>)
- !KU(<A,pk>)
- In(<A,pk>)
- K(<A,pk>) (action fact)

Public Channel:

<A,pk>

# The Language of Tamarin-Prover

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exists-trace / all-traces
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formula to prove
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The formula is given in first-order logic and uses symbols such as Ex, All, ==>, etc.

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    "
    formula to prove
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Important: In the formula we can only access action facts!

# Demo 🙂

Theory of Tamarin-Prover

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  - mathematical foundation

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    - order-sorted term algebras
    - equational theories

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  - What are the limitations of Tamarin-Prover?
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  - Implementing small toy examples to learn the language
  - Working on (parts of) the IPSec protocol

#### References

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#### Thank you for your attention!